

<b>Part B</b>	Problems 1-9 which only require answers.
<b>Part C</b>	Problems 10-15 which require complete solutions.
<b>Test time</b>	120 minutes for Part B and Part C together.
<b>Resources</b>	Formula sheet and ruler.

### Level requirements

The test consists of three written parts (Part B, Part C and Part D). Together they give a total of 54 points consisting of 22 E-, 19 C- and 13 A-points.

Level requirements for test grades

E: 14 points

D: 23 points of which 6 points on at least C-level

C: 30 points of which 11 points on at least C-level

B: 38 points of which 5 points on A-level

A: 45 points of which 8 points on A-level

The number of points you can have for a complete solution is stated after each problem. You can also see what knowledge level(s) (E, C and A) you can show in each problem. For example (3/2/1) means that a correct solution gives 3 E-, 2 C- and 1 A-point.

For problems labelled “*Only answer is required*” you only have to give a short answer. For other problems you are required to present your solutions, explain and justify your train of thought and, where necessary, draw figures.

**Write your name, date of birth and educational programme on all the sheets you hand in.**

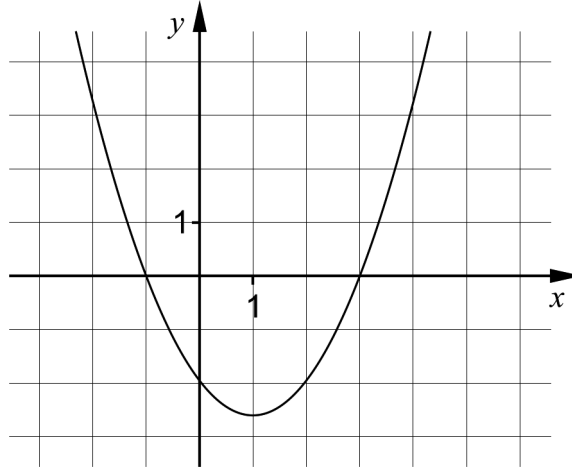
Name: \_\_\_\_\_

Date of birth: \_\_\_\_\_

Educational programme: \_\_\_\_\_

**Part B:** Digital resources are not allowed. *Only answer is required.* Write your answers in the test booklet.

1. The figure shows the graph of a quadratic function.



- a) State the zeroes of the function. \_\_\_\_\_ (1/0/0)
- b) State the equation of the symmetry line of the graph. \_\_\_\_\_ (1/0/0)

2. On Cocos the Clown's web page you can read how much it would cost to hire her for a kid's birthday party. She charges a fee of SEK 200 for her preparations and then SEK 10 per minute during the performance.

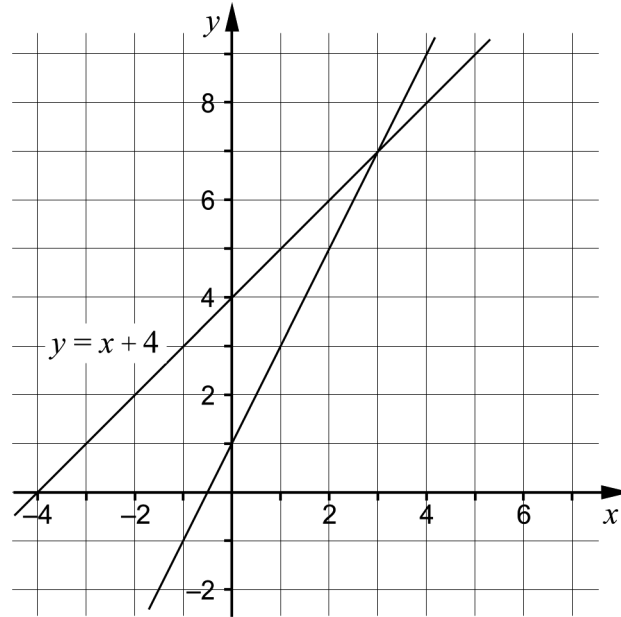


Let  $y$  be the total cost in SEK and  $x$  the time in minutes.

Write down a function on the form  $y = kx + m$  which describes how the total cost depends on the length of Cocos the Clown's performance.

\_\_\_\_\_ (1/0/0)

3. A linear system consists of two equations. The lines of the equations are drawn in the coordinate system. One of the lines has the equation  $y = x + 4$



a) State the equation of the other line in the coordinate system. \_\_\_\_\_ (1/0/0)

b) State the solution to the linear system. \_\_\_\_\_ (1/0/0)

The two lines in the linear system intersect at a point.

c) State the equation for yet another line that passes through that point. \_\_\_\_\_ (1/0/0)

4. Fill in what is missing in the box in order for the equality to be true.

$8(5 - 3x)(5 + 3x) = \square - 72x^2$  \_\_\_\_\_ (0/1/0)

5. Solve the equations.

a)  $x^{\frac{1}{4}} = 2$  \_\_\_\_\_ (1/0/0)

b)  $9^{\frac{3}{2}} \cdot 9^{\frac{x}{2}} = 9$  \_\_\_\_\_ (0/1/0)

c)  $3(3^x + 3^x + 3^x) = 3^{35}$  \_\_\_\_\_ (0/0/1)

6. Which two of the alternatives A-E equals 4?

A.  $8^{-\frac{2}{3}}$

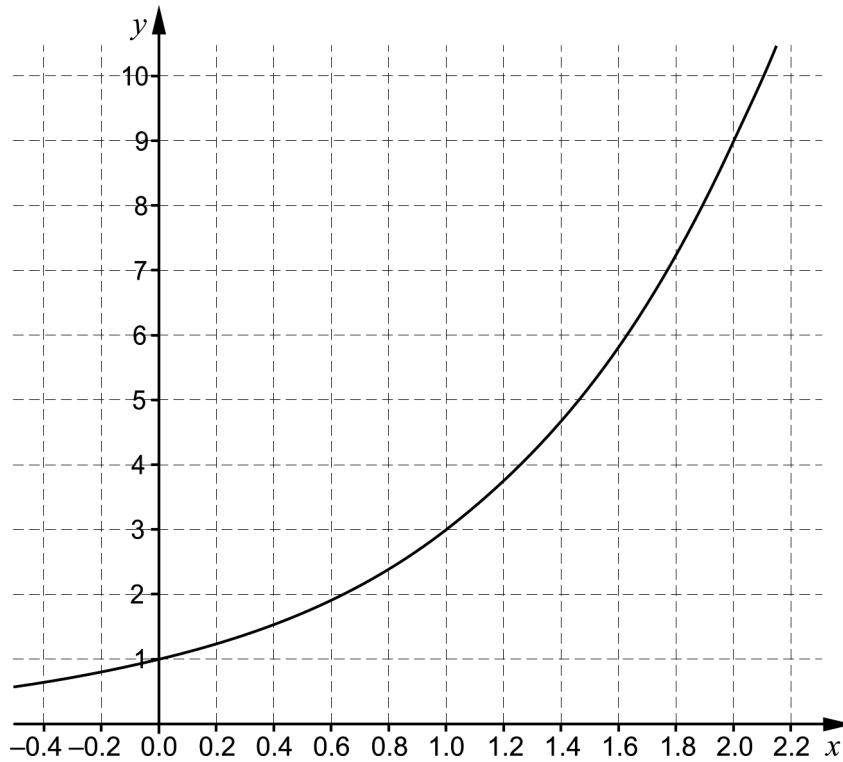
B.  $8^{\frac{1}{2}}$

C.  $8^{\frac{2}{3}}$

D.  $2 \cdot 8^{\frac{2}{4}}$

E.  $4 \cdot 8^0$  \_\_\_\_\_ (0/1/0)

7. Kalle uses graph drawing software to draw the graph of an exponential function  $f$  where  $y = f(x)$ .



- a) Use the graph and determine  $a$  if  $f(a) = 2$  \_\_\_\_\_ (0/1/0)
- b) Write down the expression for the function Kalle has drawn.  
 \_\_\_\_\_ (0/1/0)
8. The quadratic function  $f(x) = 2x^2 + 4x$  has two zeroes. One of them is  $x = -2$ . Write down the second zero.  
 \_\_\_\_\_ (0/1/0)
9. Simplify the expressions as far as possible.
- a)  $(x + 5)^2 - 10x$  \_\_\_\_\_ (1/0/0)
- b)  $(x - 3)^2 - 4(x - 3)(x + 3) + 3x^2$  \_\_\_\_\_ (0/1/0)
- c)  $(x + 1 + \sqrt{2x + 1})(x + 1 - \sqrt{2x + 1})$  \_\_\_\_\_ (0/0/1)

**Part C:** Digital resources are not allowed. Do your solutions on separate sheets of paper.

10. A straight line passes through the points  $(-8, 5)$  and  $(12, 15)$ .  
Determine the equation of the line on the form  $y = kx + m$ . (2/0/0)

11. Solve the equations algebraically.

a)  $x^2 + 4x - 12 = 0$  (2/0/0)

b)  $(x - 4)^2 = 2(x - 4)$  (0/2/0)

12. Write down an equation in the form  $y = kx + m$  for a line that is parallel to the line  $2x + y + 3 = 0$  (2/0/0)

13. Ove calculates the expression  $123456789 \cdot 123456789 - 123456788 \cdot 123456790$  on his calculator. The calculator returns the result 0.

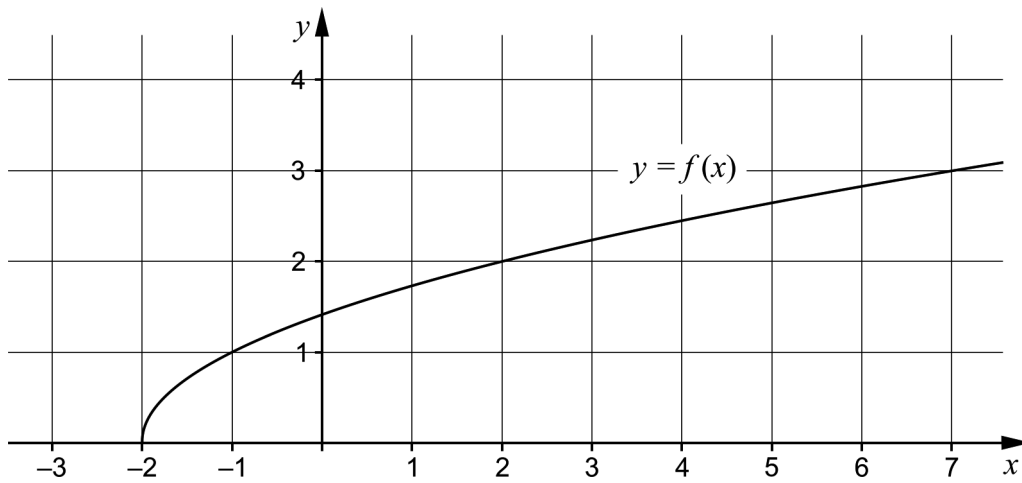


- Ove suspects that the calculator returns wrong answer. Show, by using algebra, that the calculator returns wrong answer. (0/2/0)

14. It holds for two functions  $f$  and  $g$  that  $y = f(x)$  and  $y = g(x)$ .

What values can the gradient  $k$  assume, if the graphs of the functions  $f(x) = x^2 + 4$  and  $g(x) = kx + 2$  should intersect twice? (0/0/2)

15. The figure below shows the graph of a function  $f$  where  $f(x) = \sqrt{x+2}$



- a) State the range of the function. *Only answer is required* (0/0/1)
- b) Use the graph to solve the equation  $2 \cdot f(x+2) = 6$  (0/0/1)